

Reg. No. :

**Question Paper Code : 30537**

B.E./B.Tech. DEGREE EXAMINATIONS, NOVEMBER/DECEMBER 2024

### Fifth Semester

## Electronics and Communication Engineering

EC 8553 – DISCRETE-TIME SIGNAL PROCESSING

(Common to : Biomedical Engineering/Computer and Communication Engineering/Electronics and Telecommunication Engineering/Medical Electronics)

(Regulations 2017)

Time : Three hours

Maximum : 100 marks

Answer ALL questions.

PART A — (10 × 2 = 20 marks)

1. What is the relationship between the Discrete Fourier Transform (DFT) and the Discrete-Time Fourier Transform (DTFT) and how can DFT be obtained from DTFT?
2. Find the inverse DFT of the sequence  $X(k) = \{0, 10-j10, -4, 10+j10\}$ .
3. Show the mapping of poles from s-plane to z-plane in Impulse Invariant Transformation technique.
4. Define warping effect.
5. Recall the magnitude of side lobe level of Hanning FIR window.
6. A system with transfer function  $H(z)$  has impulse response  $h(n)$  defined as  $h(2) = 1$ ,  $h(3) = -1$  and  $h(n) = 0$  otherwise. Show that  $H(z)$  is a FIR high pass filter.
7. The filter coefficient  $-0.673$  is represented by sign magnitude fixed point arithmetic. Find the quantization error due to truncation if the word length is 6 bits.
8. Find the minimum scaling factor  $S_0$  to avoid overflow  $S_0x(n)+h(n)$ , where  $x(n)=0.75$  and  $h(n)=0.45$ .
9. Define circular buffering.
10. List the advantages of fixed point architecture.

PART B — (5 × 13 = 65 marks)

11. (a) Compute the 8 point IDFT of the following sequence :

$X(k) = \{2, 1.7071 + j0.707, 1+j, 0.2929 + j0.7071, 0, 0.2929-j0.7071, 1-j, 1.7071 - j0.7071\}$  using DIF-FFT algorithm. Calculate the number of complex multiplications and additions required to compute DFT using the above algorithm and compare it with direct evaluation of DFT.

Or

- (b) Compute the Linear Convolution of the two sequences  $x[n] = \{-1, 2, -1, 0, 1, 3, -2, 1, 3, -2, -1, 0, -2\}$  and  $h(n) = \{1, 0, 1\}$  using overlap save method.

12. (a) Find the analog transfer function ( $H(s)$ ) of a Butterworth digital low pass filter using impulse invariant technique with  $T = 1$  sec satisfying the following specification :

$$0.9 \leq |H(e^{j\omega})| \leq 1 \quad 0 \leq \omega \leq 0.25\pi$$

$$|H(e^{j\omega})| \leq 0.1 \quad 0.55\pi \leq \omega \leq \pi$$

Or

- (b) Realize the direct form – I, direct form – II, cascade form and parallel form for the following system :

$$y(n) = x(n) + 2x(n-1) + \frac{3}{4}y(n-1) - \frac{1}{4}y(n-2)$$

13. (a) (i) Model the transfer function of FIR filter with minimum number of multipliers.

$$(1) \quad H(z) = 1 + \frac{2}{3}z^{-1} + \frac{15}{8}z^{-2} + \frac{2}{3}z^{-3} + z^{-4} \quad (3)$$

$$(2) \quad H(z) = 1 + \frac{3}{4}z^{-1} + \frac{17}{8}z^{-2} + \frac{4}{3}z^{-3} + z^{-4} \quad (3)$$

- (ii) Discuss the importance of rectangular window. (7)

Or

- (b) Find the filter coefficients of an ideal high pass filter with and without hamming window. Assume order of the filter  $N = 11$ .

$$H(e^{j\omega}) = \begin{cases} 0 & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 1 & \frac{\pi}{4} \leq |\omega| \leq \pi \end{cases}$$

14. (a) Examine the effect of quantization on pole locations of the given system function  $H(z) = \frac{1}{(1-0.35z^{-1})} \cdot \frac{1}{(1-0.62z^{-1})}$  in direct form and in cascade form and select the better realization form based on the output quantization noise power.

Or

- (b) Determine the limit cycle oscillations and deadband of the following first order IIR filter. Assume the truncated bit  $b = 3$ .

$$\text{Output } y(n) = x(n) - 0.95 y(n-1)$$

Input to the system is

$$x(n) = \begin{cases} 0.875 & n = 0 \\ 0 & \text{Otherwise} \end{cases}$$

15. (a) Describe the architecture of any floating point processor with suitable block diagram.

Or

- (b) Describe the DSP functionalities and circular buffering in detail.

PART C — (1 × 15 = 15 marks)

16. (a) Design a Chebyshev Type I low pass filter with  $T = 1$  sec satisfying the following constraints using Impulse Invariant Method.

$$0.8 \leq |H(e^{j\omega})| \leq 1 \quad \text{for } 0 \leq \omega \leq 0.2\pi$$

$$|H(e^{j\omega})| \leq 0.2 \quad \text{for } 0.6\pi \leq \omega \leq \pi$$

Realize the filter using cascade structure.

Or

- (b) Design a Butterworth Low pass filter with  $\omega_p = 0.23\pi$ ,  $\omega_s = 0.43\pi$ ,  $\alpha_p = 2$  dB,  $\alpha_s = 11$  dB and  $T = 1$  sec using Bilinear transformation.

Realize the filter using Direct form II structure.